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# Multilateral Index Number Methods for Consumer Price Statistics

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@TheIFS

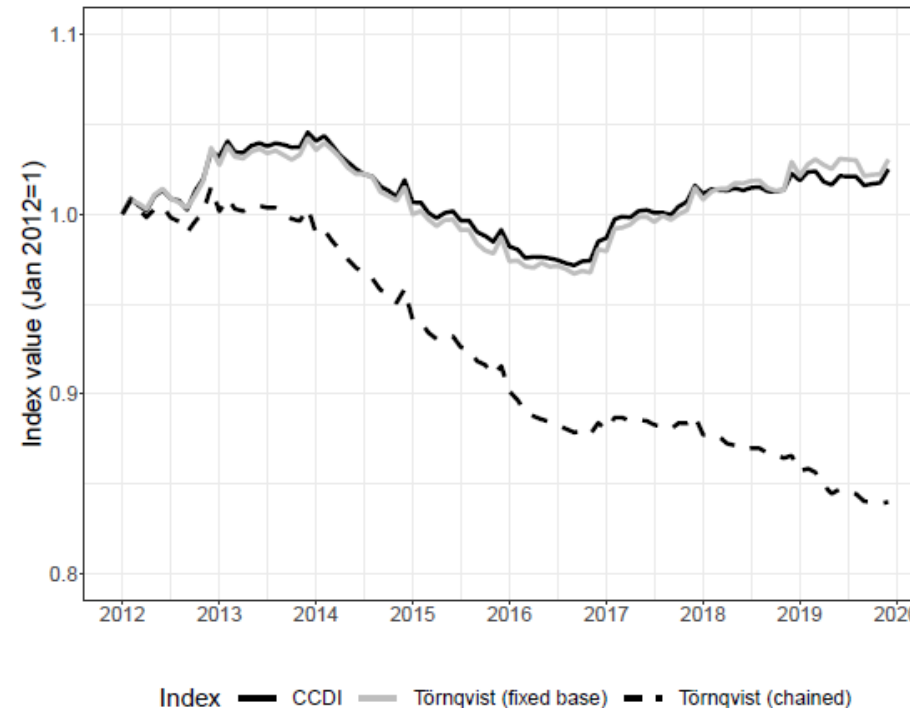


Economic  
and Social  
Research Council

- Growing interest by NSIs in using transactions level (“scanner”) data for price measurement
  - EPOS data from retailers have much larger **sample sizes** all production of index numbers at **greater frequency** than traditional price surveys
- Production of higher frequency indices (e.g. month to month price changes) creates new challenges
  - Traditional (“bilateral”) index number methods can exhibit worryingly large “chain drift”
- Engaged by ONS through ESCoE to review ONS plans for using ***multilateral index number methods*** in the CPI
  - Report: ESCoE Discussion Paper No. 2022-08 April 2022

# Why multilateral index numbers

- Chaining indexes is desirable because we want accurate measures of inflation between consecutive periods and we have product churn – don't want the basket to get out of date
- But chaining month-to-month with transaction level data can lead to massive chain drift



# Why multilateral index numbers

- Multilateral indexes introduced to this context for the purpose of controlling chain drift
- The CCDI index in the previous figure is a multilateral method calculated over the full sample
  - By definition does not suffer from chain drift bias – uses all periods of data
- With non-revisable CPIs, need a method for **extending** the series when new data is released
  - Simply expanding the window for multilateral indexes can result in a re-writing of history.
  - Extend series by splicing “windows” together so that old price comparisons are unaffected
- Extending the series reintroduces chain drift to some degree
  - Empirical question how much

- Empirically assess different **multilateral index number methods, window lengths and extension methods** using a wide variety of goods (N=178) over a long period of time (2012-2019)
  - Draw on household scanner data from the UK
  - Use IndexNumR package in R written by Graham White
- Previous work has tended to look at smaller numbers of products over short time periods (Chessa 2021, Ivancic et al. 2011, Lamboray 2017)
  - Generalisable?
- Examine sources of chain drift bias
  - We believe novel to the literature

- Confirm that bilateral indices suffer serious chain drift and that fixed base indices tend to become unrepresentative
- GEKS-Fisher and GEKS-Walsh indices largely similar to CCDI (GEKS-Tornqvist) with occasional outliers. Differences with the Geary Khamis (GK) index more substantial.
- Different extension methods associated with similar chain drift biases. GK more sensitive to choice of extension method.
- 25-month window needed when extending indices to substantially reduce chain drift
- Recommendation: CCDI index extended using mean splice and at least a 25 month window
  - CCDI-favoured relative to other GEKS indices because it is possible to impute missing prices

# Findings



- Product churn is strongly correlated with rates of chain drift bias
- High frequency (monthly) churn a problem when window lengths are short, low frequency (annual) churn still an issue for longer window lengths

# Multilateral indices

- Various options – GEKS

$$\mathbb{P}_{GEKS-F}^{\tau} = \prod_t [P_F^{\tau,t}]^{1/T} \quad \text{where } P_F^{\tau,t} \text{ is a Fisher index}$$

$$\mathbb{P}_{CCDI}^{\tau} = \prod_t [P_{Tq}^{\tau,t}]^{1/T} \quad \text{where } P_{Tq}^{\tau,t} \text{ is a Törnqvist index}$$

$$\mathbb{P}_{GEKS-W}^{\tau} = \prod_t [P_W^{\tau,t}]^{1/T} \quad \text{where } P_W^{\tau,t} \text{ is a Walsh index}$$

- Or Geary-Khamis

$$b_n = \sum_t \left( \frac{q_n^t}{q_n} \right) \left( \frac{p_n^t}{\mathbb{P}_{GK}^t} \right) \quad \text{for } n = 1, \dots, N$$

$$\mathbb{P}_{GK}^t = \frac{\mathbf{p}^{t'} \mathbf{q}^t}{\mathbf{b}' \mathbf{q}^t} \quad \text{for } t = 1, \dots, T.$$



# The linking problem

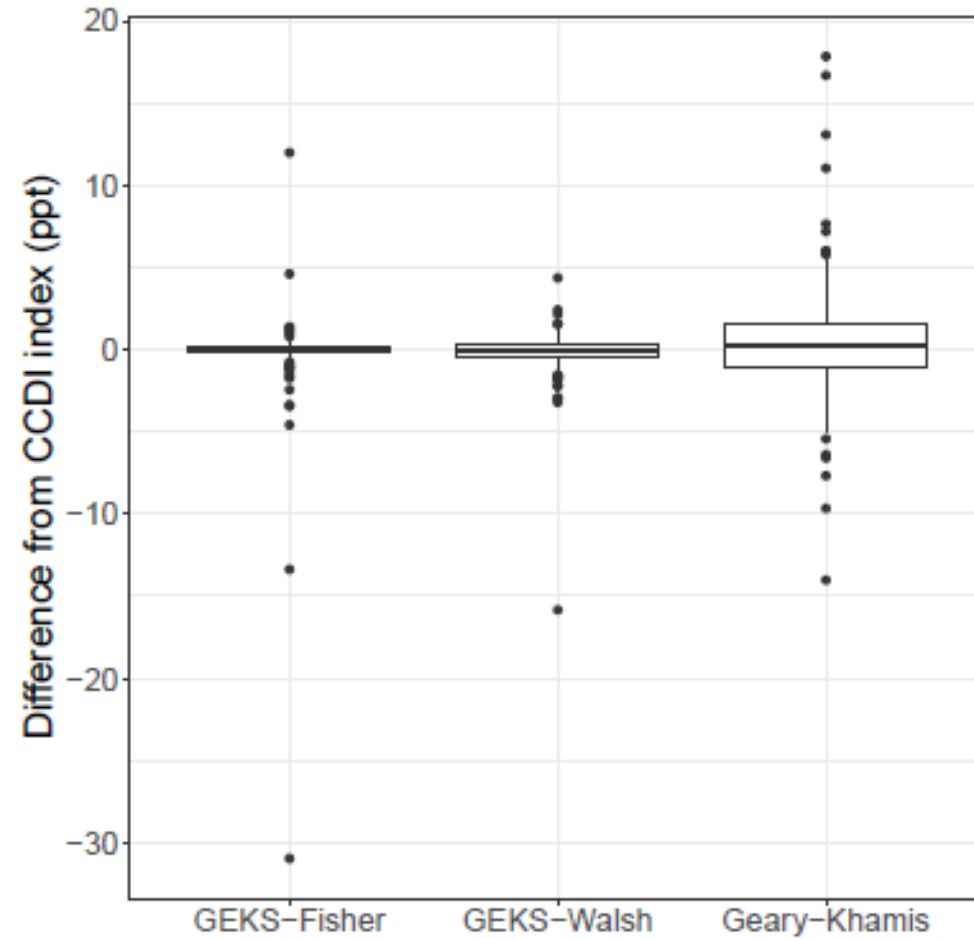
- The indices satisfy the multiperiod identity test ( $p^{1,2}p^{2,3}p^{3,1} = 1$ )
- But.. when new months are included in the index, past prices will need to be revised
- One set of solutions is *rolling window* to link indices calculated in different windows  $(1, \dots, T)$  and  $(2, \dots, T)$ 
  - “roll forward” index  $P$  by one period to get  $\tilde{P}$
  - Use an overlapping period  $s$  to extend the index

$$\rho^{T+1}(s) = \frac{\mathbb{P}_s}{\mathbb{P}_1} \frac{\tilde{\mathbb{P}}^{T+1}}{\tilde{\mathbb{P}}^s}$$

- Rolling window approaches use different splice periods,  $s$  (window, half, movement etc.)
  - Mean splice takes geometric average using all possible splicing periods
- Other extension methods are possible (and we include)

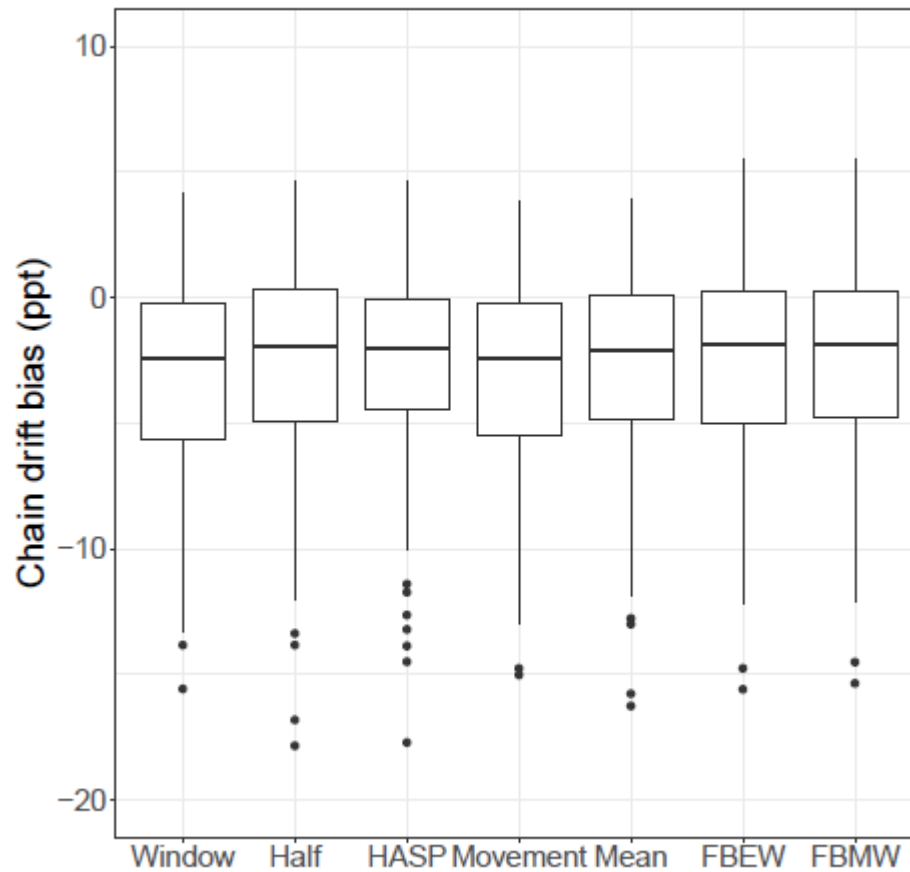
- Splicing allows the index to be updated without altering the series that has been published
- But reintroduces chain drift
- We assess chain drift bias across different indices, window lengths and extension methods
- Bias defined in Fisher sense (difference between index calculated over the whole period and spliced index)

# Comparison of different indices (using all periods)

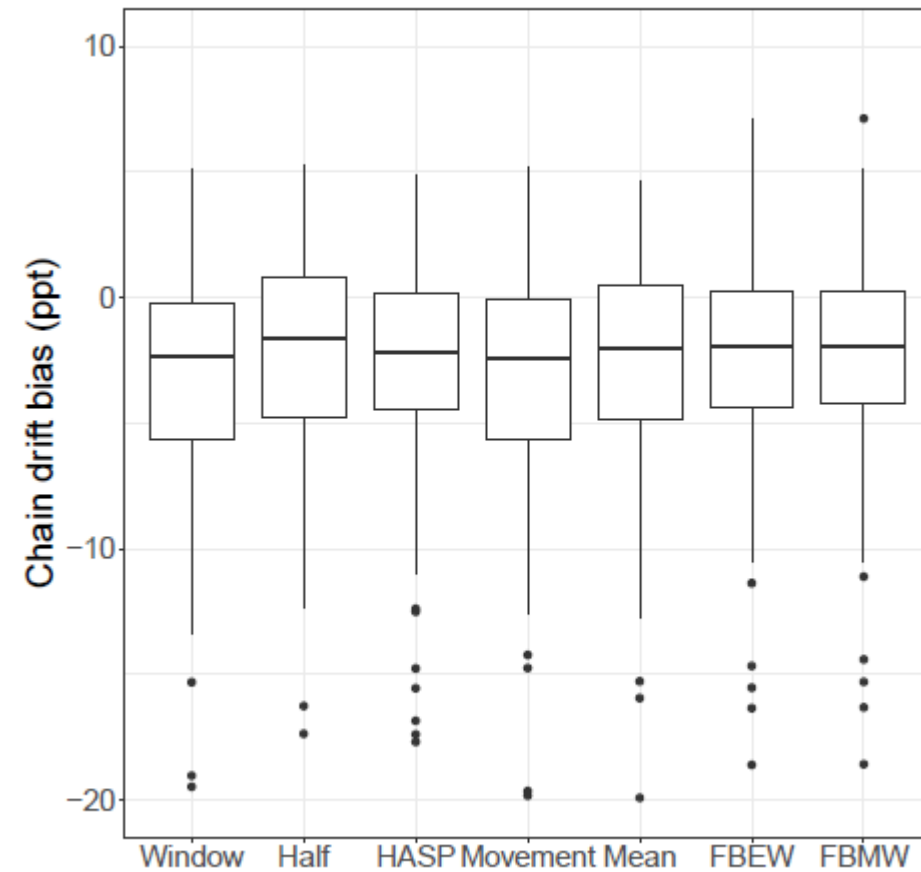


# Chain drift bias with different splicing methods (13 month window)

(a) CCDI

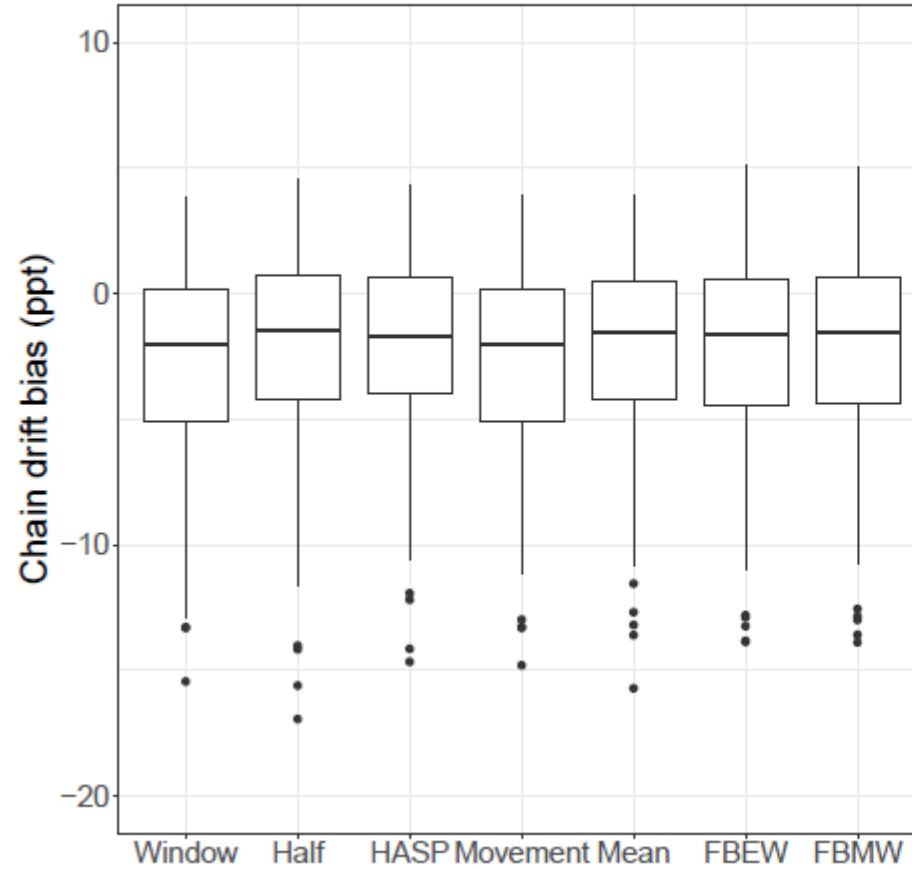


(b) GEKS-Fisher

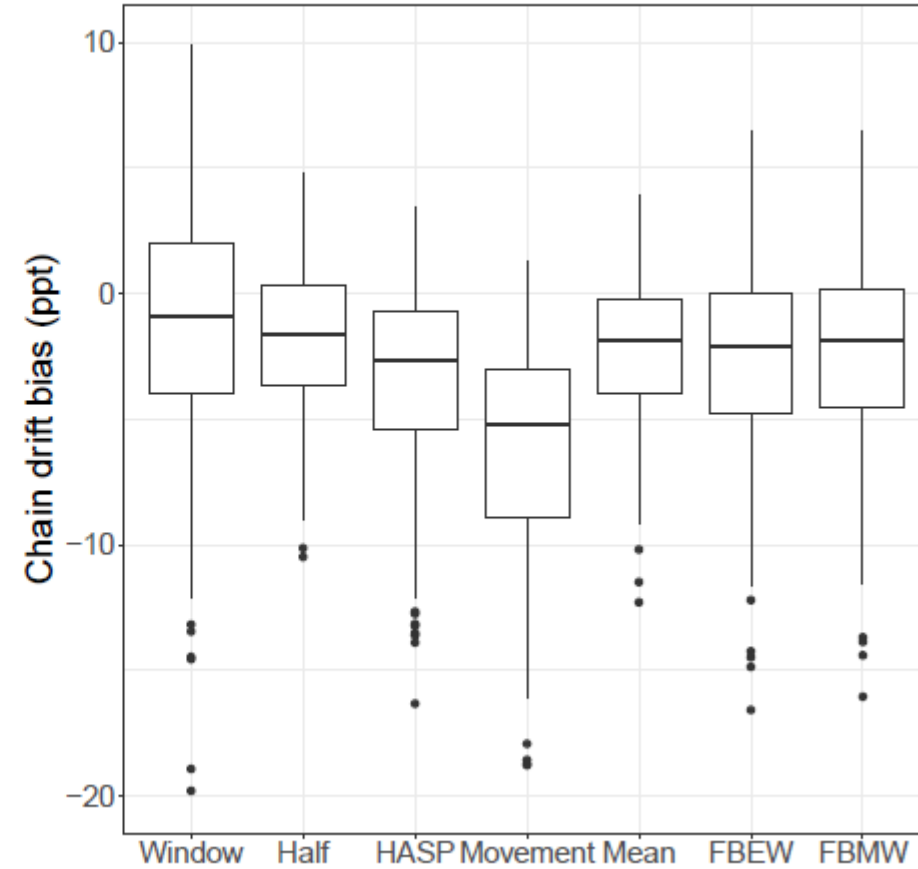


# Chain drift bias with different splicing methods (13 month window)

(c) GEKS-Walsh

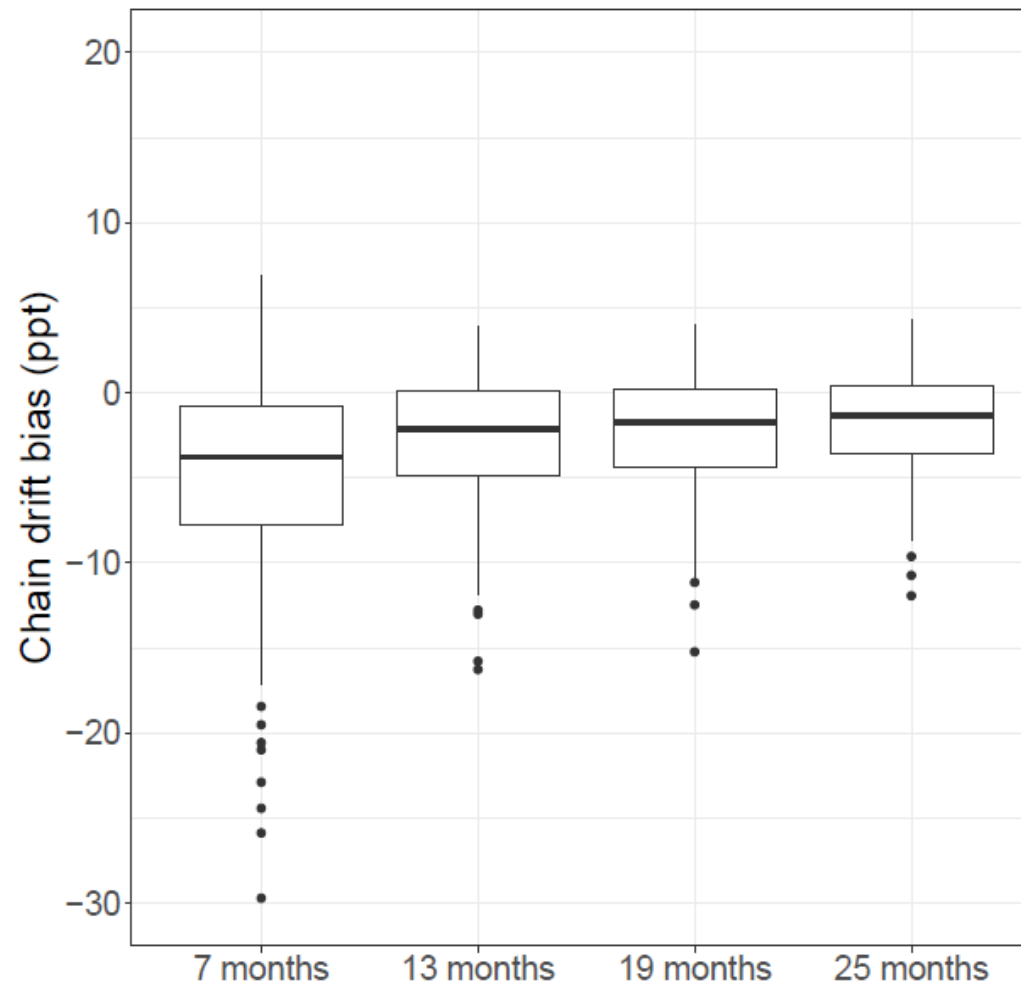


(d) GK



# Chain drift bias using different window lengths (mean splice)

(a) CCDI



# Possible determinants of chain drift bias

- **Regress absolute chain drift bias on ...**
- **Monthly churn:** share of spending on products in the current month that were not observed purchased in the previous month
- **Annual churn:** share of spending on products in the current year that were not observed purchased in the previous year (e.g. run-out sales Melser and Webster (2021))
- **Seasonality in pricing ('weak seasonality'):** estimated from fixed effects regressions of log prices on monthly dummies
- **Proportion of products on price promotion each year**
- **Proportion of products on quantity promotion each year**

# Determinants of chain drift bias (7 month window length)

|                     | CCDI                | GEKS-Fisher         | GEKS-Walsh          | GK                  |
|---------------------|---------------------|---------------------|---------------------|---------------------|
|                     | (1)                 | (2)                 | (3)                 | (4)                 |
| Pricing seasonality | −0.022<br>(0.110)   | 0.006<br>(0.117)    | 0.017<br>(0.095)    | 0.015<br>(0.099)    |
| Quantity promotions | −0.105*<br>(0.059)  | −0.099<br>(0.063)   | −0.086*<br>(0.051)  | −0.125**<br>(0.053) |
| Price promotions    | 0.030<br>(0.041)    | 0.031<br>(0.043)    | 0.019<br>(0.035)    | 0.024<br>(0.037)    |
| Annual churn        | 0.479***<br>(0.107) | 0.479***<br>(0.113) | 0.425***<br>(0.092) | 0.389***<br>(0.095) |
| Monthly churn       | 0.497**<br>(0.243)  | 0.478*<br>(0.257)   | 0.458**<br>(0.211)  | 0.640***<br>(0.217) |
| Observations        | 175                 | 175                 | 175                 | 175                 |
| R <sup>2</sup>      | 0.202               | 0.181               | 0.213               | 0.220               |

*Note: All indexes are extended using the mean splice. \* $p < 0.1$ ; \*\* $p < 0.05$ ; \*\*\* $p < 0.01$*



# Determinants of chain drift bias (25 month window length)

|                     | CCDI                | GEKS-Fisher         | GEKS-Walsh          | GK                |
|---------------------|---------------------|---------------------|---------------------|-------------------|
|                     | (1)                 | (2)                 | (3)                 | (4)               |
| Pricing seasonality | 0.001<br>(0.048)    | 0.023<br>(0.053)    | 0.001<br>(0.045)    | −0.028<br>(0.033) |
| Quantity promotions | −0.009<br>(0.027)   | −0.021<br>(0.030)   | −0.006<br>(0.026)   | −0.023<br>(0.018) |
| Price promotions    | −0.024<br>(0.019)   | −0.037*<br>(0.021)  | −0.031*<br>(0.018)  | −0.001<br>(0.012) |
| Annual churn        | 0.149***<br>(0.046) | 0.154***<br>(0.052) | 0.129***<br>(0.044) | 0.061*<br>(0.033) |
| Monthly churn       | 0.075<br>(0.108)    | 0.078<br>(0.122)    | 0.022<br>(0.103)    | 0.140*<br>(0.074) |
| Observations        | 175                 | 175                 | 175                 | 175               |
| R <sup>2</sup>      | 0.110               | 0.100               | 0.085               | 0.073             |

*Note: All indexes are extended using the mean splice. \* $p < 0.1$ ; \*\* $p < 0.05$ ; \*\*\* $p < 0.01$*

# Conclusions and directions for future research

- Recommend the use of the CCDI index with mean splice and 25 month window
  - GEKS Fisher appears to have occasional outliers
  - Can use imputation for missing prices
- When does product missingness become a problem?
- Does the timing of product entry and exit affect the optimal splicing period/method?
- More empirical examination of “similarity” linking methods

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